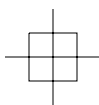


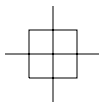
Normality and the Process Behavior Chart

Donald J. Wheeler



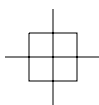
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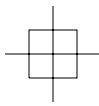




Contents

About the Author	<i>v</i>
One The Problem	1 - 4
Two The Normal Distribution	5 - 20
2.1 De Moivre's Binomial Approximation	5
2.2 Laplace's Error Distributions	8
2.3 Laplace's Limit Theorem	10
2.4 Bessel's Verification	12
2.5 Quetelet's Fallacy	13
2.6 Galton and the Quincunx	16
2.7 Summary	19
Three Are the Data Normally Distributed?	21 - 40
3.1 The Quincunx Data: Part One	21
3.2 The Quincunx Data: Part Two	24
3.3 Could the Data be Normally Distributed?	27
3.4 Quetelet's Chest Size Data Revisited	29
3.5 Bessel's Data Revisited	31
3.6 The Quincunx Data: Part Three	32
3.7 Are the Data Normally Distributed?	34
3.8 Summary	38
Four Shewhart's Solution	41 - 56
4.1 Three Types of Cause-and-Effect Relationships	41
4.2 Learning from Data	46
4.3 The Average and Range Chart	48
4.4 The Chart for Individual Values	52
4.5 Shewhart's Solution	55





Five	The Scaling Factors	57 - 76
	5.1 From Summary Statistics to Three-Sigma Limits	57
	5.2 More About the Bias Correction Factors	63
	5.3 How Many Data Are Needed for the Limits?	68
	5.4 Normality and the Scaling Factors	74
Six	Three-Sigma Limits	77 - 96
	6.1 Three-Sigma Limits	77
	6.2 How Do Three-Sigma Limits Work?	81
	6.3 A Broader Investigation	83
	6.4 Average Run Lengths	90
	6.5 The Effects of Degrees of Freedom Upon ARL_0	93
Seven	Normality and the Process Behavior Chart	97 - 100
	Appendix	101 - 146
	More About the 1143 Distributions	103
	100 Binomial Distributions	105
	112 Poisson Distributions	107
	43 Gamma Distributions	109
	100 F-Distributions	111
	398 Beta Distributions	113
	41 Weibull Distributions	115
	349 Burr Distributions	117
	Three Regions of the Shape Characterization Plane	123
	Tables	131 - 146
	A.1 Percentiles of Chi-Square distributions	131
	A.2 Areas Under the Standard Normal Curve	132
	A.3 Charts for Individual Values and Moving Ranges	134
	A.4 Average and Range Charts Using the Average Range	136
	A.5 Average and Range Charts Using the Median Range	138
	A.6 Average and Standard Deviation Charts	
	Using the Average Standard Deviation	140
	A.7 Average and Standard Deviation Charts	
	Using the Median Standard Deviation	142
	A.8 Bias Correction Factors	144
	Index	147

